

Consider a 120cm wide slab of Pu^{239} with the following characteristics:

$$\sigma_f = 1.85 \text{ b} \quad \sigma_a = 2.11 \text{ b} \quad \sigma_{tr} = 6.8 \text{ b} \quad \nu = 2.98 \quad \eta = 2.61$$

$$N(\text{Pu}^{239}) = 0.00395 \times 10^{24}$$

1. Analytical approach.

- Calculate the effective k value for the geometry and material composition. Classify this setup as subcritical, critical, or supercritical.
- Analytically determine and plot the SS flux distribution for the critical case (solution given in text).

2. Numerical approach.

- Numerically determine and plot the SS flux distribution for the critical case using the Gauss Siedel or SOR method.

Use the following error criterions for flux and k:

$$\text{flux error} = \frac{\sum_{i=1}^{\# \text{ nodes}} \text{flux}^{new} \& \sum_{i=1}^{\# \text{ nodes}} \text{flux}^{old}}{\sum_{i=1}^{\# \text{ nodes}} \text{flux}^{old}} \quad (\text{ }_{100} < 0.0001$$

$$k \text{ error} = \frac{k^{new} \& k^{old}}{k^{old}} \quad (\text{ }_{100} < 0.0001$$

- Numerical Set up:
- use 10 grids i.e. set delta x = 12
 - use an initial flux of 1.0 in all grids
 - use an initial guess of k=0.7

HINT : you will have two iterative loops, an “inner” loop which is the Gauss Siedel iteration for the flux, given a k value, and an “outer” loop which will update and converge on the value of k. Consider combining the two iterations.

Normalize the solutions to have a maximum flux of 1.0. Please hand in a copy of your source code.

- Compare the effective k value calculated analytically and numerically. Compare the flux distributions calculated analytically and numerically.

3. Calculate the transient solution using the semi-implicit method. Plot the center line flux and k as a function of time. Compare this to a plot of the center line flux as a function of iterations for Question 2. For this transient solution, devise a “controller” to adjust k so that a steady state is reached.